

# CS 520: Introduction to Artificial Intelligence

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Lecture 5:

Game playing

## Review: Constraint Satisfaction

- **Given:**
  - A set of variables:  $x_1 \dots x_n$
  - A finite domain of values for each variable:  
 $D_1 \dots D_n$
  - A set of constraints:  $C_1 \dots C_m$
- **Find:** An assignment of values to variables that satisfies the constraints.

# Review

- **Examples of Constraint Satisfaction Problems**
  - N-Queens.
  - House Floorplanning.
  - Job scheduling.
  - Crypt-Arithmetic.
  - Scene Labeling.
  - VLSI Layout and routing.
  - Graph Coloring.
  - Bin Packing.
- **Arity**

# Review

## Constraint propagation

- **Remove values from domain that are ruled out by constraints**
  - **Constraint:**  $A > B$
  - **Domains:**  $A: \{3, 5, 7\}, B: \{4, 6, 8\}$
  - **Arc consistency:**  $A: \{5, 7\}, B: \{4, 6\}$
- **Full propagation can be multi-step**
  - **Constraints:**  $A > B, B > C$
  - **Domains:**  $A: \{3, 5, 7\}, B: \{4, 6, 8\}, C: \{5, 7\}$
  - **Full propagation:**  $A: \{7\}, B: \{6\}, C: \{5\}$

# Review

## CSP Algorithms

- **Simple backtrack:**
  - Test only at leaves
- **Backtrack with early pruning:**
  - Test each constraint as soon as its vars are set
- **Forward checking**
  - When assign variable, establish arc consistency of new value with all unassigned variables
- **Full lookahead**
  - When assign variable, do full constraint propagation

## Another Alpha Prune

