Composing Controllers for Team Coherence
Maintenance with Collision Avoidance

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by

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Abstract

Many multi-agent applications may involve a notion of spatial coherence. For instance, simulations of virtual agents often need to model a coherent group or crowd. Alternatively, robots may prefer to stay within a pre-specified communication range. This work proposes an extension of a decentralized, reactive collision avoidance framework, which defines obstacles in the velocity space, known as Velocity Obstacles (VOs), for coherent groups of agents. The extension, referred to in this work as a Loss of Communication Obstacle (LOCO), aims to maintain proximity among agents by imposing constraints in the velocity space and restricting the set of feasible controls. If the introduction of LOCOs results in a problem that is too restrictive, then the proximity constraints are relaxed in order to maintain collision avoidance. A weighted velocity selection scheme is utilized in order to steer agents towards their goals, as well as agents which are farther away and thus might be violating proximity constraints. The approach is fast and integrates nicely with the Velocity Obstacle framework. It is shown to yield improved coherence for groups of robots connected through an input constraint graph, while moving with constant velocity. The approach is evaluated for collisions, computational cost and proximity constraint maintenance through a series of simulated environments, which have single and multiple team variations. The experiments show that improved coherence is achieved while maintaining collision avoidance, at a small computational cost and path quality degradation.

In order to experimentally validate new algorithms, such as the LOCO approach, having a software infrastructure capable of running a plethora of algorithms on many agents is needed. When moving from virtual agents to robotic systems, these algorithms take the form of a controller. Composing various controllers together to
create a diverse testbed environment is also essential for the development process of new algorithms. Thus, this work additionally describes a software infrastructure for developing controllers and planners for robotic systems, referred to here as PRACSYS. At the core of the software is the abstraction of a dynamical system, which, given a control, propagates its state forward in time. The platform simplifies the development of new controllers and planners and provides an extensible framework that allows complex interactions between one or many controllers, as well as motion planners. For instance, it is possible to compose many control layers over a physical system, to define multi-agent controllers that operate over many systems, to easily switch between different underlying controllers, and plan over controllers to achieve feedback-based planning. Such capabilities are especially useful for the control of hybrid and cyber-physical systems, which are important in many applications. The software is complementary and builds on top of many existing open-source contributions. It allows the use of different libraries as plugins for various modules, such as collision checking, physics-based simulation, visualization, and planning. This work describes the overall architecture, explains important features and provides use-cases that evaluate aspects of the infrastructure.
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Chapter 1 Introduction

This chapter introduces the two major contributions of this work: team coherence and controller composition. The aim of this chapter is to help familiarize readers with the material and to provide an outline of the structure of the thesis.

1.1 Team Coherence and Collision Avoidance

There are many practical applications of decentralized collision avoidance techniques. For instance, crowd simulations often have hundreds of agents moving in a dynamically changing environment. While it is important for agents to not collide with each other and the obstacles, in order to run the simulation in real time, it is also equally important to reduce all communication overhead. However, sometimes only providing decentralized collision avoidance may not be sufficient, as some applications may involve a secondary objective, where teams of agents need to maintain a certain level of coherence. Coherence often implies that the agents should remain within a certain distance of one another. In games and simulations, the agents may need to remain within a certain distance because of implied social interactions, or because they need to reach their destination together so as to be more effective in completing an objective at their goal. For instance, a team of agents in a game will be more effective in attacking an enemy if all the units move together against the opponent and do not split into multiple groups. In mobile sensor networks, robots may have to respect radial communication limits.

The Velocity Obstacle (VO) formulation [14, 43, 51] is a framework for reactive collision avoidance. It is fast as it operates directly in the velocity space of each agent. It is also a decentralized approach as each agent reasons independently about its controls, as long as it can compute the position and velocity of its neighbors. There is also anonymity between robots, as the framework does not have to reason about specific agents, which is an important distinction for computational efficiency.
Current work in Velocity Obstacles does not directly address the issue of coherence. Consider the situation in Figure 1.1, where two agents are required to avoid an obstacle and reach their desired destination. An application of the basic VO framework may result in the two agents splitting and passing the obstacle from opposite ends. It would be desirable, however, for the agents to select, in a decentralized manner, a single direction to follow so as to avoid the obstacle and reach their goal while maintaining coherence. The decentralized nature of the solution will be especially helpful in robotic applications because no communication will be required between robots. It will also provide improved scalability in simulations and games.

Figure 1.1: Two agents navigating around a static obstacle: (a) the agents split to reach their goals without collisions, while in (b) the agents move together as a coherent team. The second behavior must be achieved in a decentralized manner.

This work proposes a method for maintaining team coherence within the VO framework in a decentralized manner. The desired coherence for a problem can be defined as a graph of dependencies between agents. An edge in the graph implies that the corresponding agents should remain within a predefined distance as they move towards their goal. Given this input graph, an agent constructs an additional obstacle in the velocity space for each neighbor with which it wants to maintain connectivity. This construction is referred to in this work as a Loss of Communication Obstacle (LOCO).
Building on top of the VO framework allows LOCOs to focus on coherence maintenance, rather than obstacle avoidance. In order to construct the LOCO, the assumption is that a neighbor will maintain its current control, as in the original VO framework. Then, a LOCO defines the set of velocities that will lead the two agents to be separated beyond a desired distance within a certain time horizon. A scheme is proposed for integrating information from the multiple VOs defined for collision avoidance and the LOCOs defined for coherence maintenance. If the set of velocities that satisfy both constraints is not empty for a satisfactory time horizon, then the velocity in this set that brings the agent closer to its goal is chosen. A valid velocity implies that, given the neighbor does not change control, following this velocity will not lead the agent into a collision or violation of proximity constraints for the given horizon. If the set of valid velocities is empty, then the objective of maintaining coherence is dropped in favor of guaranteeing collision avoidance, which should be satisfiable, unless oscillations appear in the selected controls of agents. If two agents that are supposed to retain proximity end up violating the distance constraint, the proposed method makes them move in a direction that will allow them to reconnect.

This work describes the LOCO method and provides simulations which show that, by reasoning about distance constraints, it is possible to solve decentralized collision avoidance problems while improving the coherence of a team. The approach is built on top of and compared against a formulation of velocity obstacles proposed in the literature for teams of agents that execute the same protocol, referred to as Reciprocal Velocity Obstacles [43, 51]. The experiments consider disk-shaped agents that move with a constant speed in a holonomic manner, i.e., the agents can freely choose to follow any direction instantaneously. First, a series of static environments are tested with a single team of agents navigating while maintaining coherence. Different types of proximity constraints between team members are considered. Then, tests for multiple teams of agents navigating in the same environment while maintaining coherence are performed.
1.2 Composition and Evaluation of Controllers

Developing and evaluating control or motion planning methods can be significantly assisted by the presence of an appropriate software infrastructure that provides basic functionality common among many solutions. At the same time, new algorithms should be thoroughly tested in simulation before being applied on a real system. Physics-based simulation can assist in testing algorithms in a more realistic setup so as to reveal information about the methods helpful for real world application. These realizations have led into the development of various software packages for physics-based simulation, collision checking and motion planning for robotic and other physical systems, such as Player/Stage/Gazebo [20], OpenRAVE [10], OMPL [19], PQP [17], USARSim [7]. At the same time many researchers interested in developing and evaluating controllers, especially for systems with interesting dynamics, often utilize the extensive set of MatLab libraries.

There are numerous problems which require the integration of multiple controllers or the integration of higher-level planners with control-based methods. For instance, controlling cyber-physical systems requires an integration of discrete and continuous reasoning, as well as reasoning over different time horizons. Similarly, a problem that has attracted attention corresponds to the integration of task planners with motion planners so as to solve challenges that are more complex than the traditional Piano Mover’s Problem. At the same time, higher-dimensional and more complex robotic platforms, including humanoid systems and robots with complex dynamics, are increasingly becoming the focus of the academic community.

This work builds on top of many existing contributions and provides an extensible control and planning framework that allows for complex interactions between different types of controllers and planners, while simplifying the development of new solutions. The focus is not on providing implementations of planners and controllers but defining an environment where new algorithms can be easily developed, integrated in an object-oriented way and evaluated. In particular, the proposed software
platform, referred to here as **PRACSYS**, offers the following benefits:

- **Composability:** **PRACSYS** provides an extensible, composable, object-oriented abstraction for developing new controllers and simulating physical systems, as well as achieving the integration of such solutions. The interface is kept to a minimum so as to simplify the process of learning the infrastructure.

- **Ease of Evaluation:** The platform simplifies the comparison of alternative methodologies with different characteristics on similar problems. For instance, it is possible to evaluate a reactive controller for collision avoidance against a replanning sampling-based or search-based approach.

- **Scalability:** The software is built so as to support lightweight, multi-robot simulation, where potentially thousands of systems are simulated simultaneously and where each one of them may execute a different controller or planner.

- **New Functionality:** **PRACSYS** builds on top of existing motion planning software. In particular, the OMPL [19] library focuses on single-shot planning but **PRACSYS** allows the use of OMPL algorithms on problems involving replanning, dynamic obstacles, as well as extending into feedback-based planning.

- **ROS Compatibility:** The proposed software architecture is integrated with the Robotics Operating System (ROS) [55]. Using ROS allows the platform to meet a standard that many developers in the robotic community already utilize. ROS also allows for inter-process communication, through the use of message passing, service calls, and topics, all of which **PRACSYS** takes advantage of.

- **Pluggability:** **PRACSYS** allows the replacement of many modules through a plugin support system. The following modules can be replaced: collision checking (e.g., PQP [17]), physics-based simulation (e.g., Open Dynamics Engine [47]), visualization (e.g., OpenSceneGraph [32]), as well as planners (e.g., through OMPL [19]) or controllers (e.g., Matlab implementations of controllers).

After reviewing related contributions, this thesis outlines the software architecture and details the two main components of **PRACSYS**, simulation and planning. The thesis also provides a set of use-cases that illustrate some of the features of the software
infrastructure and gives examples of various algorithms that have been implemented with the assistance of PRACSYS.
Chapter 2  Background

This chapter gives crucial background information on the two major parts of this work: decentralized collision avoidance with team coherence and controller composition.

2.1  Team Coherence and Collision Avoidance

There are many related works that arise when dealing with notions of teams and providing collision avoidance. These works are categorized and described in the following subsections.

2.1.1 Virtual Agent Applications

The need to move multiple agents as a coherent team arises in many virtual agent applications [36, 46], ranging from crowd simulation [35], to pedestrian behavior analysis [34, 37], to shepherding and flocking behaviors [27, 53].

Many methods make use of “steering behaviors”, with the objective of having agents navigate in a life-like and improvisational manner [40]. These steering behaviors are separated into three categories: separation alignment, and cohesion. Using combinations of these steering behaviors, it is possible to achieve higher-level goals, such as “get to the goal and avoid all obstacles”, “follow this path”, or “join a group of characters”. These higher-level behaviors are particularly useful for objectives such as simulating realistic crowd interactions [39]. An alternative method is the social force model [18], which shares a similar goal of trying to achieve realistic interactions.

2.1.2 Coupled Multi-Robot Path Planning

There is also extensive literature on motion coordination and collision avoidance in robotics. The multi-robot path planning problem can be approached by either a coupled approach or a decoupled one [23, 24]. The coupled approach plans for the composite robot, which has as many degrees of freedom as the sum of degrees of freedom
of each individual robot. Integrated with complete/optimal planners, the coupled algorithm achieves completeness/optimality. Nevertheless, it becomes intractable due to its exponential dependency on the number of degrees of freedom.

2.1.3 Decoupled Multi-Robot Path Planning

Decoupled approaches plan for each agent individually. In prioritized schemes, paths are computed sequentially and high-priority agents are treated as moving obstacles by low-priority ones [12]. Searching the space of priorities can assist in performance [5]. Such decoupled planners tend to prune states in which higher priority agents allow lower priority ones to progress, which may eliminate the only viable solutions. Search-based decoupled approaches consider dynamic prioritization and windowed search [42], as well as spatial abstraction for improved multi-agent heuristic computation [45,54]. In particular, mobile robotic sensor networks require that robots move while maintaining communication. Techniques which attempt to tackle this issue have to balance a trade-off between centralized and decentralized planning. There are techniques that create networks of robots to compute plans in a centralized manner across distributed systems [8] or in a fully decentralized manner [4].

2.1.4 Formations

There is a significant amount of work on formation control, which is a way of moving multiple agents as a coherent team. One direction is to use a virtual rigid body structure to define the shape of a formation, and then plan for this rigid body [25]. Other techniques attempt to have more flexible structures, where interactions between robots are modeled as flexible joints [2]. An alternative is to first generate a feasible trajectory for the group’s leader according to its constraints and then use feedback controllers for the followers [3, 13]. This work, however, does not share the same objectives as standard formation approaches.
2.1.5 Reactive Obstacle Avoidance

Many techniques attempt to solve the problem of collision avoidance using reactive methods. One technique used in robotics is the Dynamic Window approach, which operates directly in the velocity space of a robot, reasoning over the achievable velocities within a small time interval [15]. An alternative approach, known as the Velocity Obstacle (VO), assumes that neighboring agents will keep following their current control. Based on this assumption, it defines conic regions in velocity space, which are invalid to follow, as they lead to a collision with the neighbor at some time in the future [14]. If the future trajectory of other robots is known, non-linear VO can be constructed [22]. The basic VO formulation can result in oscillations in motion when multiple agents execute the same algorithm. The reciprocal nature of other robots can be taken into account in order to avoid these oscillations, which leads to the definition of Reciprocal Velocity Obstacles [51]. Using this idea of reciprocity, the robots can attempt to optimally steer out of collision courses with other robots using an extension of this framework called Optimal Reciprocal Collision Avoidance (ORCA) [50]. This technique was extended to 3D cases using simple-airplane systems [44]. Further work extends the VO formulation to work with acceleration constraints as well as many kinematically and dynamically constrained systems [52].

2.1.6 Control-Based Obstacle Avoidance

A common control-based method is the Receding Horizon technique, which has been applied to this problem [26]. Another technique employed to retain safety is the use of a roundabout policy, which ensures collision avoidance between robots that follow the same policy. Such policies have been proven to be safe under certain conditions, where the robots are modeled as hybrid systems [48]. A generalized roundabout policy has been proven safe for an arbitrarily large number of robots has been proposed, but the formal verification of liveness for the policy has not been provided [33]. To address the liveness issue of this policy, further work adds minimal communication between the robots to derive a dynamic priority scheme, ensuring that at least one robot is
making progress towards its goal at all times [21].

2.1.7 Contribution

A major part of this work involves using a reactive technique to define new obstacles in the velocity space, called Loss of Communication Obstacles (LOCO). LOCOs are computed quickly and, when integrated with Velocity Obstacles, allow robots to reactively avoid static and dynamic obstacles while maintaining a better sense of coherence. The new technique does not impose communication requirements, yet maintains connectivity in a decentralized manner. This approach utilizes a weighted velocity selection method in order to move agents towards their goals, while also pushing agents towards each other if they start to move farther apart. LOCOs do not introduce any new requirements or assumptions. The approach requires that robots are able to sense the position and velocity of other robots in the scene, as well as the position of static obstacles, which are all previous requirements and assumptions from the VO framework.

2.2 Controller Composition and Simulation Environments

The Robot Operating System (ROS) [55] is an architecture that provides libraries and tools to help software developers create robotic applications. It provides hardware abstractions, drivers, visualizers, message-passing and package management. PRACSYS builds on top of ROS and utilizes its message-passing and package management. ROS was inspired by the Player/Stage combination of a robot device interface and multi-robot simulator [16]. Gazebo is focusing on 3D simulation of multiple systems with dynamics [20]. Although PRACSYS shares similar objectives with Gazebo, the former focuses mostly on a control and planning interface that is not provided by Gazebo.

There is a series of alternative simulators, such as USARSim [7], the Microsoft Robotics Developers studio [29], UrbiForge [49], the Carmen Navigation Toolkit [6], Delta3D [9] and the commercial package Webots [28]. Most of these systems focus on modeling complex systems and robots and not on defining a software infrastructure.
for composing and integrating controllers and planners for a variety of challenges.

Other software packages provide support for developing and testing planners. For instance, Graspit! [30] is a library for grasping research, while OpenRAVE [10] is an open-source plugin-based planning architecture that provides primitives for grasping and motion planning for mobile manipulators or full-body humanoid robots. The current project shares certain objectives with tools, such as OpenRAVE. Nevertheless, the definition of an extensible, object-oriented infrastructure for the integration of controllers, as well as the integration of planners with controllers to achieve feedback-based planning, are unique features of PRACSYS. Furthermore, multiple aspects of OpenRAVE, such as the work on kinematics, are complementary to the objectives of PRACSYS and could be integrated into the proposed architecture. The same is true for libraries focusing on providing prototypical implementations of sampling-based motion planners, such as the Motion Strategy Library (MSL) [41] and the Open Motion Planning Library (OMPL) [19]. In particular, OMPL has already been integrated with PRACSYS and is used to provide concrete implementations of motion planners. The proposed infrastructure, however, allows the definition of more complex problems than the typical single-shot motion planning challenge, including challenges such as planning among moving obstacles.

The second contribution of this work involves the development of a platform for composing and evaluating controllers and motion planners. This platform, called PRACSYS utilizes a framework which allows both high level and low level controllers to be composed in a way that provides complex interactions between many agents. In addition to the LOCO algorithm being written and implemented in PRACSYS, a set of use cases highlighting the scalability, pluggability, robustness, and composability of the platform is provided.
Chapter 3 Decentralized Team Coherence Maintenance under the Velocity Obstacle Framework

This chapter contains information about the LOCO algorithm. It provides a definition of the problem, a description of the VO framework, the details of the LOCO algorithm, how the VOs and LOCOs are integrated, and finally the velocity selection scheme.

3.1 Problem Statement

Consider $n$ planar, holonomic disks moving with constant speed $s$. Let the set of all agents be $A$. Each disk agent $a \in A$ has radius $r_a$ and can instantaneously move with a velocity vector $v_a$ that has magnitude $s$. Agents are assumed to be capable of sensing the position and velocity of other agents in the environment within a sensing radius $d_{\text{sense}}$. Furthermore, the agents have available a map $M$ of the environment that includes the static obstacles. The configuration space for each agent is $Q = \mathbb{R}^2$, and it can be partitioned into two sets, $Q_{\text{free}}$ and $Q_{\text{obst}}$, where $Q_{\text{free}}$ represents the obstacle free part of the space, and $Q_{\text{obst}}$ is the part of the space with obstacles. Each agent follows a trajectory $q_a(t)$, where $t$ is time. Initially an agent is located at a configuration $q_a(0) = q_{a,\text{init}}$ and has a goal location $q_{a,\text{goal}}$.

Consider the distance $d(a, b, t)$ between agents $a$ and $b$ at time $t$ (Figure 3.1). If $d(a, b, t) < r_a + r_b$, then agents $a$ and $b$ are said to be in collision at time $t$. Collisions with static obstacles occur when $q_a(t) \in Q_{\text{obst}}$. An input graph $G(A, E)$ is provided that specifies which agents need to be in close proximity. The vertices of graph $G$ correspond to the set of agents $A$ and an edge $(a, b)$ implies that agents $a$ and $b$ must satisfy $d(a, b, t) \leq d_{\text{prox}}$, where $d_{\text{prox}}$ is a proximity constraint.

The objective is for the agents to move from $q_{a,\text{init}}$ to $q_{a,\text{goal}}$ without any collisions with obstacles or among them, while satisfying as much as possible the proximity constraints specified in the input graph $G$. More formally, all agents should follow
Figure 3.1: Agents $a$ and $b$ share a proximity constraint $d_{prox}$. Agent $a$ moves with velocity $v_a$ where $\|v\| = s$ and can sense all agents within $d_{sense}$.

Trajectories $q_a(t)$ for $0 \leq t \leq t_{final}$, so that $\forall \ a \in A$:

- $q_a(0) = q_{a}^{\text{init}}$
- $q_a(t_{\text{final}}) = q_a^{\text{goal}}$
- $q_a(t) \in Q_{\text{free}}, \forall \ t \in [0, t_{\text{final}}]$
- and $\forall \ b : r_a + r_b < d(a, b, t) < D$, where
  - $D = d_{prox}$, if $\exists (a, b) \in E$ of graph $G$,
  - and $D = \infty$ otherwise.

### 3.2 Velocity Obstacle Framework

Velocity obstacles are defined in the relative velocity space of two agents. $VO_{a \parallel b}^{\infty}$ can be geometrically constructed as in Figure 3.2. Agent $a$’s geometry is reduced to a point by performing the Minkowski sum of agent $a$ and agent $b$: $a \oplus b$. Then, tangent lines to the Minkowski sum disk $a \oplus b$ are constructed from agent $a$. These tangent lines bound a conic region. This region represents the space of all velocities $v_a$ of agent $a$ that would eventually lead into collisions with agent $b$ assuming that $b$ has zero velocity. Given that agent $b$ has a velocity $v_b$, the conic region needs to be translated by the vector $v_b$. This construction assumes an infinite time horizon. In practice, it is often helpful to truncate the VO based on a finite time horizon $\tau$. This $VO$ represents all velocities $v_a$, which will lead into a collision within time $t \leq \tau$, given
Figure 3.2: Construction of $VO_{a|b}^\infty$ for an infinite time horizon. The Minkowski sum of $a$ and $b$, $a \oplus b$ is used to define a cone in velocity space, which is then translated by $v_b$. The shaded region represents all velocities $v_a$, which lead $a$ into collision with $b$.

that agent $b$ keeps moving with velocity $v_b$.

This work adopts a modification of the basic VO framework, which deals with the case that the two agents are reciprocating [51]. Reciprocal Velocity Obstacles (RVOs) are created by translating the VO according to a weighted average of the agents’ velocities, $(\alpha \cdot v_A) + ((1 - \alpha) \cdot v_B)$ where $\alpha$ is a parameter representing the level of reciprocity between agents $A$ and $B$. If both agents are equally reciprocal, then $\alpha = 0.5$.

Given this framework, an algorithm for calculating valid velocities for decentralized collision avoidance can be defined. Agent $a$ will have a set of reachable velocities and the task is to select one such velocity, which is collision-free. For holonomic disk agents moving at constant speed $s$, the set of reachable velocities would be $V_{reach} = \{v ||v|| = s\}$. Let the set of velocities which are invalid according to all the VO$s$ for neighbors of $a$ be defined as follows: $V_{inv} = \{v| \exists VO_{a|b} \text{ s.t. } v \in VO_{a|b}, b \in A, a \neq b\}$. Then, the set of feasible velocities which are reachable but not in the invalid set is defined as $V_{feas} = V_{reach} \setminus V_{inv}$. The selected velocity should be feasible, $v \in V_{feas}$, and typically minimizes a metric relative to the preferred velocity $v_a^{pref}$, e.g., a velocity vector that points to the goal. More details will be provided regarding the specific velocity selection scheme used in this work, in section 3.5.
Figure 3.3: Construction of $\text{LOCO}_{a|b}^\tau$ and $\text{VVC}_{a|b}^\tau$. The circular region represents the viable velocities to maintain $d(a, b, t) \leq d_{\text{prox}}$ for time horizon $\tau$. The shaded region outside the disk represents invalid velocities for agent $a$.

### 3.3 Loss of Communication Obstacles

The proposed approach extends the VO framework by creating new obstacles in the velocity space. These obstacles aim to prevent loss of communication, or more generally, to satisfy proximity constraints between agents in the form $d(a, b, t) \leq d_{\text{prox}}$ for agents $a$ and $b$ for at least a finite time horizon $\tau$. The $\text{LOCO}$ imposed by agent $b$ on agent $a$ for a horizon $\tau$, denoted as $\text{LOCO}_{a|b}^\tau$, is the set

$$\text{LOCO}_{a|b}^\tau = \{ v \mid \forall t \in [0, \tau] : d(a, b, t) \leq d_{\text{prox}} \},$$

under the assumption that agent $b$ follows its current velocity $v_b$ for at least time $\tau$.

Assume agents $a, b \in A$ for which $(a, b) \in E$ of the input graph $G$. The relative position of agent $b$ for agent $a$ will be denoted as $q_{ab} = q_b - q_a$. If the relative position at time $t$ is $q_{(ab)}(t)$, then at time $t + \tau$ the relative position of the two agents is going to be:

$$q_{ab}(t + \tau) = q_{(ab)}(t) + \tau * (V_b - V_a).$$

For the two agents to be able to communicate at time $t + \tau$, it has to be that:

$$(q_{ab}^X(t + \tau))^2 + (q_{ab}^Y(t + \tau))^2 \leq d_{\text{prox}}^2 \Rightarrow \quad (q_{ab}^X(t) + \tau * (V_b^X - V_a^X))^2 + (q_{ab}^Y(t) + \tau * (V_b^Y - V_a^Y))^2 \leq d_{\text{prox}}^2 \Rightarrow$$
\[
\left( \frac{q_{ab}^X(t)}{\tau} + V_b^X - V_a^X \right)^2 + \left( \frac{q_{ab}^Y(t)}{\tau} + V_b^Y - V_a^Y \right)^2 \leq \left( \frac{d_{prox}}{\tau} \right)^2 \Rightarrow \\
\left( V_a^X - \frac{q_{ab}^X(t)}{\tau} - V_b^X \right)^2 + \left( V_a^Y - \frac{q_{ab}^Y(t)}{\tau} - V_b^Y \right)^2 \leq \left( \frac{d_{prox}}{\tau} \right)^2
\]

The last expression implies that the velocity \( V_a \) of agent \( a \) has to be within a circle with center \( (q_{ab} + V_b) \) and radius \( \frac{d_{prox}}{\tau} \). This circle will be referred to as the valid velocity circle \( (\text{VVC}_{a|b}) \) and is the complement of the \( \text{LOCO}^\tau_{a|b} \). Figure 3.3 gives an example of a \( \text{VVC} \) circle.

An agent \( a \), however, may have multiple neighbors leading to the definition of multiple \( \text{LOCOs} \) and \( \text{VVCs} \). A choice that is made for simplicity is to consider the same time horizon \( \tau \) for the definition of all the \( \text{LOCOs} \) for all the neighbors. Then, the set of velocities \( v_a \) that will not allow \( a \) to maintain connectivity with at least one neighbor \( b \) in the graph \( G \) is the union of individual \( \text{LOCOs} \):

\[
\text{LOCO}^\tau_a = \bigcup_{\forall \ b \mid \exists (a,b) \in E} \text{LOCO}^\tau_{a|b}
\]

There are two complications arising from this definition. Firstly, it is not straightforward to compute the longest horizon for which this union is not the entire plane, i.e., the longest horizon for which the intersection of \( \text{VVCs} \) is not empty. The problem is that both the centers and the radii of the \( \text{VVCs} \) are changing for different time horizons. Secondly, the resulting region is rather complex to describe, as it corresponds to multiple circle intersections. This representation can impose significant computational overhead when the \( \text{LOCOs} \) are integrated with \( \text{VOs} \).

Instead of computing the exact intersection of \( \text{VVCs} \), this work proposes a conservative approximation that is easier to represent and beneficial for computational purposes. The approximation of the valid set of velocities corresponds to a circle inside the intersection of \( \text{VVCs} \). Figure 3.4 illustrates the procedure for two and three neighbors.
Figure 3.4: The conservative approximation of VVC in the velocity space of agent $a$ for two (left) and three (right) neighbors. The white circle corresponds to velocities that are guaranteed to maintain connectivity with the neighbors for time $\tau$.

Given two circles with centers $C_b$ and $C_c$ and radii $r_b$ and $r_c$, the inscribed circle of their intersection has the following radius and center:

$$r_{bc} = \frac{r_b + r_c - ||C_b, C_c||}{2}$$

$$C_{bc} = C_b + (r_b - r_{bc}) \frac{C_c - C_b}{||C_b, C_c||}$$

The procedure works in an incremental manner. First it computes the inscribed circle $(C_{bc}, r_{bc})$ of the intersection of two VVCs, and then computes the inscribed circle of $(C_{bc}, r_{bc})$ with another VVC and so on.

### 3.4 Integration of VOs and LOCOs

The final step for computing the LOCO is to select a suitable time horizon. A tuning approach over consecutive simulation steps is used. Given the horizon $\tau$ from the previous time step, the LOCO is computed as in Figure 3.4. Then the set $V_{valid} = V_{reach} \setminus \text{LOCO}$ is computed, which considers the reachable controls that do not violate the LOCO constraints. This operation can be done in an efficient manner especially for systems with constant speed $s$, as it corresponds to a circle to circle intersection. In the general case for systems with varying velocity there are still computational advantages, as the circular representation of the VVC greatly increases the speed in which $V_{valid}$ can be computed. Once $V_{valid}$ is available for a given $\tau$, the measure
Figure 3.5: An example of how changing the horizon affects the set of feasible controls. The left image has a larger value for $\tau$ while the right has a smaller value of $\tau$. Larger values of $\tau$ provide stronger guarantees for communication maintenance, but make finding a feasible control more difficult.

The absolute value of $|V_{\text{valid}}|$ is compared against a predefined threshold $|V_{\text{thresh}}|$. If $|V_{\text{valid}}| < |V_{\text{thresh}}|$, then $\tau$ is decreased and $V_{\text{valid}}$ is recomputed. A smaller $\tau$ implies that a bigger set of valid velocities for proximity maintenance will be returned that provides guarantees for a shorter horizon. Alternatively, if $|V_{\text{valid}}| > |V_{\text{thresh}}|$, then $\tau$ is increased. This will return a smaller set of valid velocities but will provide guarantees for a longer horizon. This tuning process continues until $V_{\text{valid}}$ comes close to $V_{\text{thresh}}$, but this takes place over multiple simulation steps and adapts on the fly to changes in the relative configuration of agents. The effects of tuning $\tau$ can be seen in Figure 3.5.

Once $\text{LOCO}_{a}$ has been computed, it must then be included in the list of constraints in order to correctly compute $V_{\text{feas}}$, which is now redefined to be $V_{\text{feas}} = V_{\text{valid}} \setminus V_{\text{inv}}$, as in Figure 3.5. Sometimes, the additional constraints imposed by $\text{LOCOs}$, cause $V_{\text{feas}}$ to become empty. In this situation, the $\text{LOCO}$ constraints are ignored, as attempting to maintain communication may be perilous to the agent’s safety.

### 3.5 Velocity Selection

Each agent has a preferred velocity it would like to follow, denoted as $v_{a}^{\text{pref}}$ for agent $a$. Ignoring the proximity constraints and in obstacle-free environment, the preferred
velocity should be in the direction of the goal configuration \( v_{goal} = q_{goal}^a - q_a \). If there are obstacles, however, setting the goal velocity in the same manner can lead the agents into local minima, causing the agent to become stuck behind the obstacle. This work avoids this issue by computing a discrete wave-front function in environments with obstacles. The goal velocity is computed as the direction to the cell with the minimum distance to the goal within a \( 3 \times 3 \) region from the current cell of the agent.

In order to account for agents violating proximity constraints, a weighted velocity selection scheme is employed that takes neighbors into account. For some agent \( a \), let \( d_i \) be the distance from agent \( a \) to another agent \( i \) and \( X_i \) be the state of agent \( i \), where agent \( i \) is part of the proximity graph of agent \( a \). Then, for \( n \) agents in the proximity graph of agent \( a \), the average weighted configuration can be computed as:

\[
q_{avg} = \frac{\sum_{i}^{n} d_i}{\sum_{i}^{n} d_{prox}} q_i
\]

Then, \( d_{avg} = ||q_a - q_{avg}|| \) is the distance between agent \( a \) and \( q_{avg} \). Let \( v_{avg} = q_{avg} - q_a \) be the vector pointing to \( q_{avg} \), and let \( v_{goal} \) be the vector towards the goal computed through the wavefront. Then, agent \( a \)'s preferred velocity is computed as follows:

\[
v_{pref}^a = \frac{d_{avg}}{d_{prox}} v_{avg} + \frac{d_{prox} - d_{avg}}{d_{prox}} v_{goal}
\]

Thus, agents which are farther away from their proximity constraints (i.e., have violated constraints) will be inclined to shorten this distance, whereas agents that have not violated any proximity constraints move towards their goals.

Once \( v_{pref}^a \) is computed, it can be checked for validity given the set \( V_{feas} \). If \( v_{pref}^a \) is feasible, then agent \( a \) will use it. In the case that \( v_{pref}^a \) is not in \( V_{feas} \), a different feasible control must be computed. In the general case, the region \( V_{feas} \) defines an area in velocity space which must be searched to find a control. The control found is the velocity \( v \in V_{feas}^a \) which minimizes distance between \( v \) and \( v_{pref}^a \).

The distance metric used in this approach is the Euclidean distance in the velocity space. Other metrics for finding the distance between velocities in this space are possible [52]. A list of intersections of the boundaries of the RVOs with \( V_{reach}^a \) is
generated and a rotational sweep algorithm determines which points are valid. These points define the boundaries of the $V_{feas}^a$ regions. They are checked to find which one of them minimizes the distance to the preferred velocity: $\min_{v \in V_{feas}^a} [d(v, v_{a}^{pref})]$. In the general case, $V_{feas}^a$ will be a non-convex region or possibly disjoint non-convex regions in the velocity space where a variant of the simplex algorithm can be used to find the optimum.

In the event that there is no valid velocity available, the agent will select its current control. The reasoning behind this is that in the VO framework, after computing VOs for their neighbors, agents assume that these neighbors will not change their control. Thus, choices that keep the current velocity are preferable for this scheme.
Chapter 4  Creating an Extensible Architecture for Composing Controllers and Planners

4.1  Architecture

The proposed architecture is composed of several modules, following the architecture of the Robotic Operating System (ROS) [55]. ROS’s architecture has separate nodes launched as executables which communicate via message passing and are organized into packages, stacks, and nodes. A package is a collection of files, while a stack is a collection of such packages. Nodes are executables. PRACSYS is a stack and the nodes launched from PRACSYS are associated with a single package. PRACSYS also allows developers to integrate additional plugins into the architecture. There are three packages which run as nodes: the simulation, planning, and visualization packages. See Figure 4.1 for a visual representation of the interactions between different packages of PRACSYS. The advantage of having separate nodes is that it makes the jump to distributed computation such as on a computing grid easier.

The common package contains useful data structures, as well as mathematical tools. The utilities package contains useful algorithms, such as graph search, as well as abstractions for planning. Both the common and utilities packages use the Boost library to facilitate efficient implementations.

Figure 4.1: Package interactions. ROS nodes communicate via message passing: simulation, visualization, and planning. The common and utilities packages are dependencies of the previous three.
The higher-level packages include simulation, visualization, and planning. The simulation package has common and utilities as dependencies. The simulation package is responsible for simulating the physical world in which the agents reside and contains integrators and collision checking. The simulation package also contains many controllers which operate over short time horizons. Controllers are part of the main pipeline and are not in the planning package because they only operate over a single simulation step. The planning package is primarily concerned with controlling agents over a longer horizon, using the simulation package internally. The visualization package gives meaningful I/O between the user and the simulation, such as selecting agents and providing manual control. The planning package can have different state than the ground truth simulator, which is useful for applications such as planning under uncertainty.

PRACSYS also has an optional input package with files for loading simulations in YAML [56] format. There is also a package containing external package dependencies used by PRACSYS, such as the Approximate Nearest Neighbors library [1].

The following discussion details the capabilities of these packages, starting with the most fundamental of the three: the simulation package.

4.2 Descriptions

This section discusses the different packages of PRACSYS in further detail.

4.2.1 Ground-truth Simulation and Controller Architecture

The simulation node is the primary location for the development and testing of new controllers, and contains a set of features which are useful for developers. The following sections will go over each of these features individually.
Composability

The simulator contains several classes which are interfaces used for the development of controllers. The fundamental abstraction is the system class - all controllers and plants are systems in PRACSYS, as shown in Figure 4.2. This functionality allows for other nodes, such as planning, to reason over one or more systems without knowing the specifics of the system. The interface is the same whether planning happens over a physical plant or a controlled system, which simplifies feedback-based planning.

The interaction between systems is governed by the pipeline shown in Figure 4.3, which ensures that every system properly updates its state and control. The functions in the pipeline are responsible for the following:

1. **copy state**: receive a state from a higher-level system, potentially manipulate this state, and pass it down to lower-level systems.

2. **copy control**: receive a control from a higher-level system, potentially manipulate this control, and pass it down to lower-level systems.

3. **propagate**: propagates a system according to its dynamics (if it is a plant), or sends a propagate signal down to lower-level systems (if it is a controller).

4. **get state**: receives the state from a lower-level system. This allows higher-level systems to query for the full state of the simulation.
Figure 4.3: The core interface of a system.

The *system* class uses the *space* abstraction, which provides a way for users to define abstract spaces in a general way, allowing for scopes beyond a Euclidean space. A space is a rectangular-bounded region of \( n \) dimensions where each dimension can be Euclidean, rotational, or one component of a quaternion. The abstraction automatically provides a way to compute metrics between different points within the space. A *space point* stores the parameters of each dimension of the *space*, and can be used to represent states and controls in the *system* class.

Note that a *system* does not need to get controls from lower-level *systems*. The *system* class contains other interface functions, which primarily fall under the category of initialization, set functions, and get functions. Systems are broken into two major categories: physical plants and controllers. Physical plants are responsible for simulating the physical agents and how they move through the environment. They store geometries and have functionality to update their configurations based on states.
set through copy state. Furthermore, physical plants are governed by state-update equations of the form $\dot{x} = f(x, u)$ implemented by the propagate function.

Controllers are classified into four major types: simple, stateful, composite, and switch. These are classes that extend the abstract controller class. A **simple controller** contains a single subsystem, which is most often the plant itself, but can also be another controller. Simple controllers are useful for creating a chain of controllers, allowing for straightforward compositions. A controller which computes a motion vector along a potential field for a holonomic disk system is an example of a simple controller on top of a physical plant. In more complex compositions, controllers will also have the need to keep an internal state, separate from its subsystem. A **stateful controller** allows for an internal state, and one such example of a stateful controller is the consumer controller. The **consumer controller** simply supplies controls to its subsystem from a pre-computed plan, where its state is the point in time along the plan to extract the control. **Composite controllers**, which can have many subsystems, provide the necessary interface for controlling multiple subsystems. The simulator, for example, which is responsible for propagating systems, is a composite controller containing all controllers and plants. The final major type of controller is the **switch controller**, which behaves quite similar to a C/C++ switch statement. A switch controller operates over an internal controller state, called a mode, which determines which of its subsystems is active. For example, a switch controller could be used to change the dynamics being applied to a plant depending if it was in a normal environment or an icy environment, in which case an inactive slip-controller would be “switched” active. Developing controllers which utilize these archetypes allows for an easy way to create more complex interactions.

**High-level simulation Abstractions**

In addition to the system abstraction, there are several high-level abstractions which give users additional control over the function of the simulation. One such abstraction is the **collision checking** abstraction, which consists of an actual collision checker
and a collision list. The collision list simply describes which pairs of geometries should be interacting in the simulation, while the collision checker is actually responsible for performing the checks and reporting when geometries have come into contact. The simulator is an extension of the composite controller, but it has additional functionality and has the unique property of always being the highest-level system in the simulation. The abstraction which users are most likely to change is the application. The application class contains the simulator and is responsible for defining the type of problem that the user wants to solve.

Interaction

The simulation node can communicate with other nodes via ROS messages and service calls. For example, moving a robot on the visualization side involves a ROS service call. Similar to how a propagate signal is sent between systems, an update signal is used to change geometry configurations. Once all systems have appended to this update signal, a ROS message is constructed from it and sent to visualization in order to actually move the physical geometry. For non-physical geometries, such as additional information of a system (i.e., a robot could have a visualized vector indicating its direction), each system is responsible for making the appropriate ROS call. If a user needs additional functionality and interaction between the nodes, they only need to implement their function in the communication class and create the appropriate ROS files.

Plugin Support

Adding a new physics engine as a plugin simply involves extending the simulator, plant, obstacle, and collision checker classes. If a user does not require the use of physics simulation, they can simply disable this by omitting it from the input file. For collision checking, PRACSYS currently provides support for PQP, as well as the use of no-collision checking. Similarly, if a user would like to add a new collision checker, they only need to extend the collision checking class.
4.2.2 Planning

The planning package is responsible for determining sequences of controls for one or many agents over a longer horizon than a single simulation step. This excludes methods which use reactive control. Furthermore, planning also reasons over higher-level planning processes, such as task coordination. The planning package is divided among several modules in order to accomplish these tasks. The high-level task coordination is provided by task planners, which contain motion planners for generating sequences of controls given a world model. The world model is a system with a simulator as a subsystem and is responsible for providing information to the planners about the state of the simulator as well as providing additional functionality. The motion planners are the individual motion planning algorithms which compute controls. The current version of PRACSYS has certain sampling-based motion planners implemented, which use some basic modules to accomplish their specified tasks, including local planners and validity checkers. PRACSYS also integrates existing motion planning packages such as OMPL by providing an appropriate interface. The current focus of the planning package has been sampling-based methods; however, it is not limited to these types of planners and can easily support search-based or combinatorial approaches.

High-Level Abstractions

All of the abstractions described in this section interact according to Figure 4.4.

Task planners are responsible for coordinating the high-level planning efforts of the node. Task planners contain at least one instance of a motion planner and use planners to accomplish a given task. Ultimately, the goal of planning is to come up with valid trajectories for one or many systems, which bring them from some initial state to a goal state, but the task planner may be attempting to accomplish a higher-level task such as motion coordination. In this sense, the task planners are responsible for defining the objective of the planning process, while the motion planners actually generate the plan. One example is the single-shot task planner, which allows a planner to plan until it reports it has found a specified goal. Then
the single-shot task planner forwards the plan to the simulation node. Other tasks include single-shot planning, replanning, multi-target planning and velocity tuning or trajectory coordination among multiple agents.

Figure 4.4: The general structure of the planning modules. The task planner contains multiple motion planners. The task planner also contains a world model and communicates with the simulation node.

A World Model represents the physical world as observed or known to the planner, and also extends the system abstraction. A world model contains a simulator as a subsystem, exposing the functionality of the simulator to the motion planners. World models can be used to hide dimensions of the state space from the motion planners, introduce and model the uncertainty an agent has about its environment, or removing certain agents from collision checking. Having the capability to remove dimensions from the state space is useful for planning purposes because the planning process has complexity which depends on the dimensionality of the space. This reduction will make the planning process more efficient, and is related to being able to remove some systems from collision checking. These two functions together allow a full simulation to be loaded, while allowing planning to plan for agents individually in a decoupled manner for greater efficiency.

Motion planners are responsible for coming up with trajectories for individual agents or for groups of agents. The flexibility of PRACSYS allows for planners to easily be changed from performing fully decoupled planning to any range of coupling,
including fully coupled problems. Motion planners employ the use of modules, used as a black box by the motion planner, but may have a wide variety of underlying implementations available to accomplish the task. Furthermore, because of the flexibility of the system class, planners can plan over controllers as well. This allows for interesting new planning opportunities, and one example of this use is given in section 5. In this case, planners are able to essentially create trajectories through parameter space of controllers. The sampling-based planners in PRACSYS make use of four modules: local planners, samplers, distance metrics, and validity checkers. The distance metric module and the sampler module are provided by the utilities package.

**Sampling-Based Motion Modules**

**Local planners** propagate the agents according to their dynamics. PRACSYS offers two basic types of local planners, an approach local planner which uses a basic approach technique to extend trajectories toward desired states, and a kinematic local planner which connects two states exactly, but only works for agents which have a two-point boundary problem solver and kinematic agents.

**Validity checkers** provide a way to determine if a given state is valid. The most basic implementation of a validity checker, which is provided with PRACSYS simply takes a state, translates it into its geometrical configuration, and checks if there is a collision between the geometry of the agents and the environment.

**Samplers** are able to generate samples within the bounds of an abstract space. Different samplers will allow for different methods of sampling, such as uniform randomly, or on a grid.

**Distance metrics** are responsible for determining the distance of points in a space. These modules may use simple interpolating methods or may be extended to be more complex and take into account invalid areas of the space.
Interaction

The planning package communicates primarily with simulation. A planning node can send messages to the simulation such as computed plans for the agents. The planning package can further send trajectory and planning structure information to visualization so users can see the results of an algorithm. The planning node also receives control signals from the simulation node, such as when to start planning.

OMPL is a software package developed for planning purposes [19]. Because of the plugin system of PRACSYS, a simple wrapper is provided around the existing OMPL implementation in order to utilize the OMPL planners within PRACSYS.

4.2.3 Visualization

The visualization node is responsible for visualizing any aspect needed by the other nodes. Users interact with the simulation environment through the visualization. This includes, but not limited to, camera interaction, screen shots and videos, and robot tracking. The visualization provides an interface to develop alternative implementations, in case users do not want to use the provided implementation based on OpenSceneGraph (OSG) [32].

4.2.4 Other PRACSYS Packages

The remaining packages provide functionality useful across the infrastructure, such as geometric calculations, configuration information, and interpolation. An important concept is the idea of a space as provided by the utilities package, which was described earlier in Section 4.1. The input package is an optional package which includes sample input for use with PRACSYS. Files are in YAML or ROS .launch format. PRACSYS also comes with an external package for carrying along external software packages, such as the Approximate Nearest Neighbors (ANN) package [1], which is useful for motion planning.
Chapter 5  Evaluation

This chapter contains the experimental results obtained from evaluating the LOCO controller in a variety of scenarios against the most relevant competing algorithm, Reciprocal Velocity Obstacles [51]. Additionally, several use cases are presented which highlight the usability and robustness of PRACSYS.

5.1  LOCO Results

The approach was implemented using a simulation software platform. Experiments were run on computers with a 3.06 GHz Intel Core 2 Duo processor and 4GB of RAM. The experiments are organized in the following manner. First, experiments were conducted using a single team of agents moving in an environment with obstacles. Then, experiments with multiple teams were run both in an obstacle-free world and in an environment with obstacles. A team of agents corresponds to a connected component of the input graph $G$. The experiments conducted compare the LOCO formulation against RVOs. The reason for comparing against RVOs, rather than other formation techniques, is due to the decentralized nature of the LOCO algorithm, which requires no additional information outside the VO framework. In addition, LOCOs utilize the notion of coherence, which is more abstract in nature than formations. Thus, RVOs are the most relevant technique to experiment against. Each experiment was measured with regards to the following metrics:

• total number of collisions during the entire experiment,
• computation time per frame,
• total time to solve the problem,
• average ratio of respected proximity links per frame,
• and number of successful runs.

For each variation of the environment, input graph $G$ and algorithm, there were 10 runs executed. Each run had a random initial $q_{init}$ and goal configuration $q_{goal}$, which,
Figure 5.1: The environments on which the experiments were executed satisfied the proximity link in the graph $G$.

### 5.1.1 Single Team

For the single team scenarios, two different environments were tested with varying numbers of agents. The PACHINKO environment uses a series of walls with small gaps (Figure 5.1 top left), and a team of 10 agents was considered in this case. The proximity graph imposed on the team is shown in Figure 5.2 top left. The WEDGE environment (Figure 5.1 top right) attempts to split the agents into two lanes. The proximity graph imposed on the team is shown in Figure 5.2 top right.

Table 5.1 shows that there is a significant improvement in terms of the percentage of links maintained by the LOCO-based approach relative to RVOs. Another interesting
Figure 5.2: Examples of input proximity graphs used in the experiments.

statistic to examine is the coherence of agents over time, shown in Figure 5.3, which
the LOCO-based approach also improves. This comes at the cost of a slightly increased
computational cost and increased time taken by the algorithm to bring all of the
agents to their goals. An example of the paths taken by 24 agents in the PACHINKO
environment is shown in Figure 5.4. Both approaches were able to solve all of the
problems and without any collision, with the exception of one experiment for the
WEDGE environment, where a single collision was reported.

<table>
<thead>
<tr>
<th></th>
<th>time per step (s)</th>
<th>collisions</th>
<th>maintained links</th>
<th>steps</th>
<th>success</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>LOCO</td>
<td>RVO</td>
<td>LOCO</td>
<td>RVO</td>
<td>LOCO</td>
</tr>
<tr>
<td>wedge grid</td>
<td>0.03964</td>
<td>0.03488</td>
<td>0.1</td>
<td>0</td>
<td>92%</td>
</tr>
<tr>
<td>pachinko train</td>
<td>0.04474</td>
<td>0.0355</td>
<td>0</td>
<td>0</td>
<td>96%</td>
</tr>
</tbody>
</table>

Table 5.1: Results for a single team.

5.1.2 Multiple Teams

The performance of LOCOs was evaluated against RVOs in a scenario involving four
teams of agents navigating in an obstacle-free environment as shown in Figure 5.1
bottom left (CROSSROADS) and for the connectivity graph for each team shown in
Figure 5.3: Coherence over time for 24 agents in the wedge grid experiment.

Figure 5.2 bottom left. There were four agents in each team. The last setup involved again four teams of agents, each one of which had six agents connected as in Figure 5.2 bottom right. This time the environment involved a random set of rectangular obstacles as in Figure 5.1 bottom right. For each of the 10 runs the rectangles were randomly placed. The results are shown in Table 5.2.

In both the random and crossroads examples, LOCOs outperform RVOs as far as connections are concerned, though oftentimes LOCOs take more time to solve the specified problem. On different problems, both approaches can take some extra time to complete the problem for two different reasons. The VOs take extra time as agents will sometimes get caught on obstacles or are pushed away from their goals by agents on other teams. LOCOs may take extra time as they spend effort navigating agents in densely-packed situations that occur at the center of the environment as they cross over. Furthermore, LOCOs exhibit a flocking behavior which sometimes causes agents to overshoot their goals.

In the random obstacle environment, LOCOs imposed a very small computational overhead. The crossroads scenario resulted in a more significant increase, because all
agents meet in the center of the environment nearly at the same point in time. This increases computational cost, as LOCOs must tune their horizon and reconnect broken proximities more frequently. In both environments, LOCOs and RVOs resulted in no collisions, with the exception of one run of RVOs in the random environment. The main focus of these results, however, is the improvement in maintained links. The LOCO-based approach maintained 95% of the proximity links, which was an improvement over RVOs. LOCOs cause a small degradation in path quality, which is measured in the number of steps it took for agents to solve the environment. In addition to this, LOCO failed to solve one of the randomly generated environments, because agents tend to spread to the edge of their proximity constraints, which may cause problems when agents move around obstacles. Overall, the results seem to validate the initial approach, as the goal of LOCOs is to maintain safety while providing better proximity maintenance is experimentally supported.

Table 5.2: Results for multiple teams.

<table>
<thead>
<tr>
<th></th>
<th>time per step (s)</th>
<th>collisions</th>
<th>maintained links</th>
<th>steps</th>
<th>success</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>LOCO</td>
<td>RVO</td>
<td>LOCO</td>
<td>RVO</td>
<td>LOCO</td>
</tr>
<tr>
<td>random</td>
<td>0.03005</td>
<td>0.02919</td>
<td>0</td>
<td>0.1</td>
<td>96%</td>
</tr>
<tr>
<td>crossroads</td>
<td>0.00564</td>
<td>0.0034</td>
<td>0</td>
<td>0</td>
<td>98%</td>
</tr>
</tbody>
</table>

Figure 5.4: An example of the paths taken by 24 agents in the **PACHINKO** environment for the RVO (left) and LOCO (right) approach.
5.2 PRACSYS Use Cases

This section provides specific examples of the features offered by PRACSYS.

5.2.1 Showing Scalability for Multiple Agents

![Figure 5.5: A plot of simulation steps vs number of plants.](image)

Scalability is important for simulation environments in which multiple agents are to be simulated at once. The PRACSYS system structure was designed with multi-agent simulation in mind. Given a very simple controller, multiple physical plants were simulated and the time for a simulation step was tracked against number of agents, as shown in Figure 5.5. The trend shows a linear increase in simulation step duration with the number of agents, even with simulations of thousands of agents. Figure 5.6 shows 3000 agents being simulated in PRACSYS.

The Velocity Obstacle (VO) Framework was introduced as a lightweight reactive obstacle avoidance technique [14]. The basic framework has been expanded upon, with such extensions as Reciprocal Velocity Obstacles (RVO) [51]. The basic VO framework as well as several extensions have been implemented in PRACSYS and have also been used in large-scale experiments.
5.2.2 Planning over Controllers using LQR Trees

Using a C/C++ interface to Octave and its control package [11], PRACSYS can utilize the optimal control guarantees of linear quadratic regulators (LQR). Octave is an open-source Matlab clone which PRACSYS can invoke Octave, meaning it can run software developed in Matlab with little or no conversion time effort. An implementation of LQR-Trees has been developed in PRACSYS [38]. This algorithm is a prototypical example of “planning over controllers” so as to provide feedback-based solutions. The created LQR-tree is sent to the simulation node for execution. The process of incorporating the LQR code into PRACSYS took a matter of minutes.

The LQR-Tree is built incrementally similarly to RRT and its variants. It begins by computing an LQR that is based around the goal region, and then using sampling trajectories until new basins can be created using time-varying LQR over trajectories which enter existing basins. The technique has been shown to probabilistically cover the space, and stores a full description of the LQR controller used to create the basin of attraction at each tree node.
The planning node can send the controller information to the simulation node. This implementation illustrates the use of LQR controllers inside a planning structure. With this kind of framework, many more complex applications can be implemented and studied. This also shows the integration of a matrix-based interpreted language, Octave, into PRACSYS.

### 5.2.3 Controller Composition in Physics-based Simulation

PRACSYS offers a unique capability of composing systems. This scheme gives users flexibility by allowing the decomposition of individual steps into separate controllers, so that they can reused and re-combined to create new functionality.

For example, the framework given in the SIMBICON project [57], in which controllers are created for controlling bipedal robots has been implemented in PRACSYS. The hierarchy of controllers for this implementation is shown in Figure 5.7. A breakdown of this hierarchy is as follows:

![Diagram of controller composition](image)

**Figure 5.7**: A visual representation of the controller composition for controlling a bipedal robot
ODE Simulator: The simulator, using the Open Dynamics Engine. **Finite State Machine (FSM):** Several FSMs, implemented with switch controllers, sit below the simulator. Each FSM corresponds to a particular bipedal gait, such as running or skipping. Changes in the state of the simulation eventually cause a switch in the used gait. **Bipedal PD Controller:** Several PD controllers sit underneath each FSM, and represent a specific part of a gait, such as being mid-stride or having both feet planted. **Bipedal Plant:** This is the physical representation of the robot, and contains the geometry and joint information, as well as the actual dynamics of the plant.

Because ODE focuses on quick simulation for real-time applications, interactive applications can be created while sacrificing as little realism as possible. This lightweight implementation allows users to interact with this physically simulated world in interesting ways, such as manually controlling a plant among many other plants being controlled through various means. An example as shown in the submission’s video shows a toy car controlled by a user interacting with the bipedal system, described previously.

### 5.2.4 Integration with Octave, OMPL, and MoCap Data

**PRACSYS** has been integrated with several other software packages in order to extend its functionality. **PRACSYS** has been integrated with Octave, OMPL, and motion capture data from CMU. **Motion Capture** data is used to animate characters in a realistic manner, and **PRACSYS** has integrated motion capture data from CMU. A controller which reads motion capture data has been utilized, and it reads and assigns the data to a control space point, where it is passed to the plant with copy control. The plant connected to this controller simulates a skeleton, which interpolates the configuration of each of its bones.
Chapter 6  Discussion and Future Work

The work presented in this thesis has a wide variety of possible extensions. This chapter presents a set of directions to consider for future work, in addition to discussing the two contributions.

6.1  LOCO

This work provides the formal definition for a new kind of obstacle in the velocity space of moving agents, referred to as a Loss of Communication Obstacle (LOCO), which correspond to proximity constraints with neighboring agents. These obstacles can be easily computed and integrated into the existing framework of Velocity Obstacles for decentralized collision avoidance. Additionally, an approach for tuning the time horizon parameter for these obstacles over multiple simulation steps is provided. These additional constraints increase the overall coherence of teams of agents while navigating through environments with static obstacles and other moving bodies. LOCOs can be dropped if it is determined that it is too difficult to maintain proximity without jeopardizing safety. The implementation of the technique shows improved coherence for agents who share communication links without sacrificing safety at a small computational overhead.

A natural extension is to consider more challenging systems, including kinematically and dynamically constrained systems. Adapting LOCOs to work in these cases is possible, as there have already been extensions on using VOs with dynamics. Since these extensions are in an orthogonal direction to the LOCO algorithm, it is possible to consider an integrated solution towards decentralized coherence maintenance for dynamic systems. Further extending the work to applications of real robots will require introducing a method for handling sensor errors, as well as creating a more robust reconnection strategy built on this error model. One drawback of reactive techniques is that they may get stuck in local minima. It is interesting to better
study the integration with the wavefront approach or another global planner so as to guarantee that agents will make progress towards their goal while guaranteeing safety and connectivity. A global planner can also improve the performance of the reconnection strategy. Currently, the direction to the agent with which connectivity has been lost ignores the existence of local obstacles. Another interesting direction is to study reciprocity tuning. More constrained agents, such as those who create a bridge for two otherwise disconnected agents, may be less able to reciprocate than others. Further reducing the computational overhead of the technique would also have great benefits, since larger-scale tests could be performed and have practical application areas, as in crowd simulation and video games.

6.2 PRACSYS

PRACSYS is an extensible environment for developing and composing controllers and planners with a broad range of applications. It can support multi-agent simulations, physics-based tools, and can incorporate Matlab code, the OMPL library [19] and MoCap data. There are multiple important future steps for PRACSYS. One direction is to utilize principles of software engineering to improve the generality of the system class. For example, the system class could be modeled using the blackboard architectural model, which is designed to handle complex, ill-defined problems. Another alternative is the use of design patterns, such as the composite and module structures, which would further increase the extensibility of the system class. One of the current pursuits is the development of a communication node, which simulates communication protocol parameters and failures between agents by employing a discrete event network simulator, such as ns3 [31]. This will allow the simulation of distributed planning involving communication on a computing cluster. Furthermore, a sensing node is developed for simulating sensor data in place of a physical sensor. This objective, as well as allowing algorithms coded on PRACSYS to run on physical systems, will be assisted by a tighter integration with the latest versions of Gazebo [20], OpenRave [10] and by utilizing existing ROS functionality [55].
Bibliography


